

1D Time-Dependent Problems (Galerkin method)

PDEs:

$$\begin{aligned} C_{11} \frac{\partial U_1}{\partial t} + \dots + C_{1N} \frac{\partial U_N}{\partial t} &= \frac{\partial A_1}{\partial x}(x, t, U_1, U_{1x}, \dots, U_N, U_{Nx}) \\ &- F_1(x, t, U_1, U_{1x}, \dots, U_N, U_{Nx}) \\ &= \\ &= \\ C_{N1} \frac{\partial U_1}{\partial t} + \dots + C_{NN} \frac{\partial U_N}{\partial t} &= \frac{\partial A_N}{\partial x}(x, t, U_1, U_{1x}, \dots, U_N, U_{Nx}) \\ &- F_N(x, t, U_1, U_{1x}, \dots, U_N, U_{Nx}) \end{aligned}$$

where the C_{ij} are functions of (x, t, U_1, \dots, U_N) .

Boundary conditions (at endpoints):

$$\begin{aligned} U_1 &= FB_1(t) \\ &= \\ &= \\ U_N &= FB_N(t) \end{aligned}$$

or

$$\begin{aligned} \pm A_1 &= GB_1(t, U_1, U_{1x}, \dots, U_N, U_{Nx}) \\ &= \\ &= \\ \pm A_N &= GB_N(t, U_1, U_{1x}, \dots, U_N, U_{Nx}) \end{aligned}$$

Initial conditions:

$$\begin{aligned} U_1(x, t_0) &= U_{10}(x) \\ &= \\ &= \\ U_N(x, t_0) &= U_{N0}(x) \end{aligned}$$